## K.P.CLASSES

## 2013 - SA - 1 (MATHEMATICS )

Class - X
Time Allowed: 3 Hrs.
Maximum Marks: 90

## General Instructions:

i) All questions are compulsory.
ii) The question paper consists of 34 questions into four sections, $A, B, C$ and $D$. Section $A$ comprises of 8 questions of 1 mark each, Section B comprises of 6 questions of 2 marks each, Section $C$ comprises of 10 questions of $\mathbf{3}$ marks each and Section D comprises of $\mathbf{1 0}$ questions of $\mathbf{4}$ marks each.
iii) Use of calculators is not permitted.

## Section - A

1. The decimal expansion of the rational number $\frac{33}{2^{2} .5}$ will terminate after
a. one decimal place
c. three decimal places
b. two decimal places
d. more than 3 decimal places
2. If the HCF of 65 and 117 is expressible in the form $65 m-117$, then the value of $m$ is
a. 4
b. 2
c. 1
d. 3
3. The pair of equations $x+2 y+5=0$ and $-3 x-6 y+1=0$ have
a. a unique solution
c. infinitely many solutions
b. exactly two solutions
d. no solution
4. The value of $\left(\sin 30^{\circ}+\cos 30^{\circ}\right)-\left(\sin 60^{\circ}+\cos 60^{\circ}\right)$ is
a. -1
b. 0
c. 1
d. 2
5. The value of $\frac{\tan 30^{\circ}}{\cot 60^{\circ}}$ is
a. $\frac{1}{\sqrt{2}}$
b. $\frac{1}{\sqrt{3}}$
c. $\sqrt{3}$
d. 1
6. If $\triangle A B C$ is right angled at $C$, then the value of $\cos (A+B)$ is
a. 0
b. 1
c. 2
d. 3
7. Sides of two similar triangles are in the ratio $4: 9$. Areas of these triangles are in the ratio
a. $2: 3$
b. $4: 9$
c. $81: 16$
d. $16: 81$
8. Arithmetic mean of $1,2,3,-\cdots, n$ is
a. $\frac{\mathrm{n}+1}{2}$
b. $\frac{n-1}{2}$
c. $\frac{n}{2}$
d. $\frac{n}{2}+1$

## Section - B

9. Can the number $6^{n}, n$ being a natural number, end with the digit 5 ? Give reasons.
10. Can $x-1$ be the remainder on division of a polynomial $p(x)$ by $2 x+3$ ? Justify your answer.
11. For the pair of equations
$\lambda x+3 y=-7 ; 2 x+6 y=14$
to have infinitely many solutions, the value of $\lambda$ should be 1. Is the statement true? Give reasons.
12. Prove that $\sin ^{6} \theta+\cos ^{6} \theta+3 \sin ^{2} \theta \cos ^{2} \theta=1$
13. Prove that the line joining the mid-points of any two sides of a triangle is parallel to the third side.
14. The following table shows the weights of 12 students:
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| Weight (in kg) | 67 | 70 | 72 | 73 | 75 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Number of students | 4 | 3 | 2 | 2 | 1 |

Find the mean weight by using short-cut method.

## Section - C

15. Find the zeroes of the quadratic polynomial $x^{2}+7 x+10$, and verify the relationship between the zeroes and the coefficients.
16. Prove that $\sqrt{3}+\sqrt{5}$ is irrational.
17. For which values of $p$ and $q$, will the following pair of linear equations have infinitely many solutions?
$4 x+5 y=2$
$(2 p+7 q) x+(p+8 q) y=2 q-p+1$.
18. If $\sin (A-B)=1 / 2, \cos (A+B)=1 / 2,0^{\circ}<A+B \leq 90^{\circ}, A>B$, find $A$ and $B$.
19. In $\triangle O P Q$, right-angled at $P, O P=7 \mathrm{~cm}$ and $O Q-P Q=1 \mathrm{~cm}$ (see Fig.). Determine the values of $\sin Q$ and $\cos Q$.

20. Evaluate: $\frac{5 \cos ^{2} 60^{\circ}+4 \sec ^{2} 30^{\circ}-\tan ^{2} 45^{\circ}}{\sin ^{2} 30^{0}+\cos ^{2} 30^{0}}$.
21. A girl of height 90 cm is walking away from the base of a lamp-post at a speed of $1.2 \mathrm{~m} / \mathrm{s}$. If the lamp is 3.6 m above the ground, find the length of her shadow after 4 seconds.
22. Prove that the area of an equilateral triangle described on one side of a square is equal to half the area of the equilateral triangle described on one of its diagonals.
23. The following data gives the information on the observed lifetimes (in hours) of 225 electrical components :

| Lifetimes (in hours) | $0-20$ | $20-40$ | $40-60$ | $60-80$ | $80-100$ | $100-120$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Frequency | 10 | 35 | 52 | 61 | 38 | 29 |

Determine the modal lifetimes of the components.
24. The mean of the following frequency table is 50 . But the frequencies $f_{1}$ and $f_{2}$ in class $20-40$ and $60-80$ are missing. Find the missing frequencies.

| Classes | $0-20$ | $20-40$ | $40-60$ | $60-80$ | $80-100$ | Total |
| :--- | :--- | :---: | :--- | :---: | :--- | :--- |
| Frequency | 17 | $f_{1}$ | 32 | $f_{2}$ | 19 | 120 |

## Section - D

25. Show that the square of an odd positive integer can be of the form $6 q+1$ or $6 q+3$ for some integer $q$.
26. If the remainder on division of $x^{3}+2 x^{2}+k x+3$ by $x-3$ is 21 , find the quotient and the value of $k$. Hence, find the zeroes of the cubic polynomial $x^{3}+2 x^{2}+k x-18$.
27. Draw the graphs of the pair of linear equations $x-y+2=0$ and $4 x-y-4=0$. Calculate the area of the triangle formed by the lines so drawn and the x-axis.
28. If $\sin \theta+\cos \theta=\sqrt{3}$, then prove that $\tan \theta+\cot \theta=1$

Or
Express the ratios $\cos A, \tan A$ and $\sec A$ in terms of $\sin A$.
29. There are some students in the two examination halls $A$ and $B$. To make the number of students equal in each hall, 10 students are sent from $A$ to $B$. But if 20 students are sent from $B$ to $A$, the number of students in $A$ becomes double the number of students in $B$. Find the number of students in the two halls.
30. Prove that $\frac{\sin \theta-\cos \theta+1}{\sin \theta+\cos \theta-1}=\frac{1}{\sec \theta-\tan \theta}$, using the identity $\sec ^{2} \theta=1+\tan ^{2} \theta$.
31. If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, the other two sides are divided in the same ratio. Prove it.
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Or
The ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides.
32. $B L$ and $C M$ are medians of a triangle $A B C$ right angled at $A$. Prove that $4\left(B L^{2}+C M^{2}\right)=5 B C^{2}$.
33. If the median of the distribution given below is 28.5 , find the values of $x$ and $y$.

| Class interval | Frequency |
| :--- | :--- |
| $0-10$ | 5 |
| $10-20$ | $x$ |
| $20-30$ | 20 |
| $30-40$ | 15 |
| $40-50$ | $y$ |
| $50-60$ | 5 |
| Total | 60 |

34. The following distribution gives the daily income of 50 workers of a factory.

| Daily income in (Rs.) | $100-120$ | $120-140$ | $140-160$ | $160-180$ | $180-200$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Number of workers | 12 | 14 | 8 | 6 | 10 |

Convert the distribution above to a less than type cumulative frequency distribution, and draw its ogive.
Ans find its median.

## Answers:-

1. B
2. B
3. D
4. $B$
5. D
6. A
7. D
8. A
9. 
10. No, since degree $(x-1)=1=$ degree $(2 x+3)$.
11. No.
12. 
13. 
14. 70.25
15. The zeroes of $x^{2}+7 x+10$ are -2 and -5 .
16. 
17. $p=-1, q=2$
18. $A=45^{\circ}$ and $B=15^{\circ}$.
19. $\sin Q=\frac{7}{25}, \cos Q=\frac{24}{25}$
20. $\frac{67}{12}$
21. Shadow is 1.6 m long
22. 
23. 65.625 hours
24. $f_{1}=28$ and $f_{2}=24$.
25. 
26. $k=-9$; Quotient is $x^{2}+5 x+6$; zeroes are are $3,-2,-3$..
27. The vertices of this triangle are $B(-2,0), Q(1,0)$ and $R(2,4)$. Area $=6$ sq. units
28. 
29. 100 students in hall $\mathrm{A}, 80$ students in hall B .
30. 
31. 
32. 
33. $x=8, y=7$.
34. Table is

| Daily income (in Rs.) | Cumulative frequency |
| :--- | :--- |
| Less than 120 | 12 |
| Less than 140 | 26 |
| Less than 160 | 34 |
| Less than 180 | 40 |
| Less than 200 | 50 |

Draw ogive by plotting the points : $(120,12),(140,26),(160,34),(180,40)$ and $(200,50)$

